# Harmonic Distortion Analysis of the Output Voltage in SPWM (Unipolar) Single Phase Full Bridge Inverter

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Abstract: In this paper, a simulation of SPWM (Unipolar) strategy is presented for Single phase full bridge inverter. The model is simulated in Matlab/Simulink. For different power factor loads the % THD of the output voltage are observed. The change in modulation index (MI) and the frequency of the carrier signal  $(f_c)$  changes the % THD of the output voltage. The width of gate pulses are modulated in order to obtain controlled inverter out voltage and to reduce the harmonic content as well. A comparative study of the % THD of the output voltage for the same load when connected across a conventional inverter and across SPWM fed inverter helps to understand the performance of the inverter. In SPWM inverter, to generate the gate signals, triangle wave is the carrier wave which is compared with the reference sinusoidal wave. The frequency of the output voltage depends on the frequency of the reference wave.

*Keywords:* Sinusoidal pulse width modulation (SPWM), Unipolar, Total Harmonic distortion (THD), Order of Harmonics, lagging and leading pf loads.

# I. INTRODUCTION

Inversion is the process of conversion dc power to ac power at a required output voltage, current and frequency. A static semiconductor performs this electrical energy inverting transformation process. The inverter receives the DC power from a battery and then converts it to AC with the desirable frequency. The inverter is therefore adjustable frequency voltage source.

Inverters can be classified in two types:

- voltage sorce inverter (VSI)
- Current source inverter (CSI).

A voltage source inverter (VSI) is the one in which the DC input voltage is constant and is independent of the current drawn by the load. In VSI the dc source has small or negligible impedance. The voltage at the input terminals of inverter is always constant. A current source inverter (CSI) is fed with adjustable current from the dc source of high impedance that is from a constant dc source.

According to the connections of semiconductor devices, inverters are:

- Bridge Inverters
- Series Inverters
- Parallel Inverters

A voltage source inverter (VSI) using thyristor as a switch requires forced commutation, while the VSI in which MOSFET, GTO, IGBT, power transistors are the switching devices, self commutation with gate pulse is required for their controlled turn on and off process.

## II. SINUSOIDAL PULSE WIDTH MODULATION (SPWM)

Pulse width modulation (PWM) is a powerful technique to controlling the switching devices in inverter circuits. PWM provides a way to decrease the Total Harmonic Distortion (THD) of load current and output voltage. The THD requirement can be met more easily when the output of PWM inverter is filtered. The unfiltered output will have relatively high THD, but the harmonic will be at the much higher frequencies which can be filtered out easily.

Sinusoidal pulse width modulation (SPWM) is a very simple technique used for harmonic reduction. In this technique a carrier wave (Triangular) is compared with a reference wave (Sinusoidal) to generate the gate pulses for the inverter.

A sinusoidal reference wave  $A_c$ , reference wave with  $180^0$  phase shift  $-A_c$  and a triangular carrier wave  $A_r$  of higher frequency are compared for gate pulses. There are two important parameters in this modulation technique:

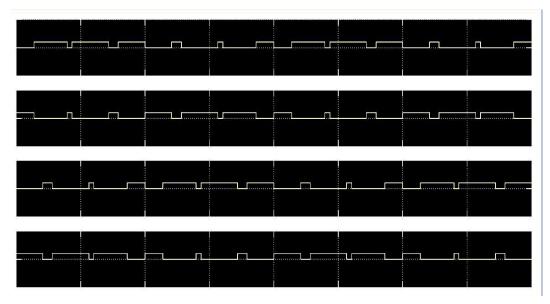
- Amplitude Modulation Ratio or Modulation Index (MI)
- Frequency Modulation Ratio

Amplitude Modulation ratio =  $\frac{A_r}{A_r}$ 

Frequency Modulation ratio =  $\frac{f_c}{f_r}$ 

The rms output voltage can be varied by varying the modulation index MI. Frequency modulation ratio changes the number of gating pulses per half cycle of the reference wave. It can be controlled by varying the frequency of carrier signal  $f_c$ . This type of modulation eliminates all harmonics less than or equal to 2P - 1. Where P is the number of pulses per half cycle  $=\frac{f_c}{2f_c}$ .

THD is a measure of closeness in shape between a waveform and its fundamental component. THD gives the information about total harmonic content, but it dose not indicate the level of each harmonic component. Lowest order harmonic (LOH) is that harmonic component whose frequency is closest to the fundamental one, and its amplitude is greater than or equal to 3% of the fundamental component.



## **III. SIMULATION RESULTS**

Fig.1: Triggering pulses for SPWM Unipolar Full Bridge Inverter

THD analysis of output voltage and current in a conventional full wave bridge inverter supplied by 240V DC source at constant load variable power factor:

| Load           | THD load current | THD output voltage |
|----------------|------------------|--------------------|
| 5kw 0 pf lag   | 12.1 %           |                    |
| 5kw 0.6 pf lag | 14.74 %          |                    |
| 5kw 0.8pf lag  | 18.66 %          |                    |
| 5kw unity pf   | 48.35 %          | 48.35%             |
| 5kw 0.8pf lead | 59.43 %          |                    |
| 5kw 0.6pf lead | 76.6 %           |                    |
| 5kw 0 pf lead  | 84.59 %          |                    |

It is clear from the above results that THD of the current depends upon the load pf. Harmonic distortion of current is high for a purely capacitive load and it is minimum for a purely inductive load. The THD of the output voltage is independent from the load power factor.

A 5 kw 0.8 lag pf load is connected to a 240V DC sources supplied single phase spwm fed unipolar full bridge inverter. For different values of carrier frequency  $f_c$  THD analysis of the output voltage is shown by the tables below:

Table 1

| For MI = 1 and $f_c = 50$ Hz<br>$V_{OUT} = 240$ volts, $(THD)_V = 48.35$ %<br>Voltage profile of the out put voltage |              |       |    |       |      |      |      |                                   |
|--|--------------|-------|----|-------|------|------|------|-----------------------------------|
| Harmonic Order   | DC component | 3     | 5  | 7     | 9    | 11   | 13   | All even order harmonics are 0.39 |
| % of fundamental   | 0.19         | 33.33 | 20 | 14.28 | 11.1 | 9.08 | 7.68 | % of fundamental component        |

Table 2

| For $f_c = 300$ Hz and MI = 0.6<br>$V_{OUT} = 105.57$ volts , $(THD)_V = 105.57$ %<br>Voltage profile of the out put voltage |   |      |      |      |       |       |       |  |
|--|---|------|------|------|-------|-------|-------|--|
| Harmonic Order   | Harmonic Order DC component 3 5 7 9 11 13 |      |      |      |       |       |       |  |
| % of fundamental   | 0   | 4.79 | 0.14 | 2.51 | 12.14 | 64.35 | 62.76 |  |

| Table  | 3 |
|--------|---|
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| For $f_c = 300$ Hz and MI = 1<br>$V_{OUT} = 188.2$ volts, $(THD)_V = 49.92$ %<br>Voltage profile of the out put voltage |              |   |   |   |   |    |    |  |
|---|--------------|---|---|---|---|----|----|--|
| Harmonic Order  | DC component | 3 | 5 | 7 | 9 | 11 | 13 |  |
| % of fundamental 0 1.28 0.95 2.18 22.27 19.08 18.06   |              |   |   |   |   |    |    |  |

Table 4

| For $f_c = 500$ Hz and MI = 0.6<br>$V_{OUT} = 147$ volts , $(THD)_V = 107.82$ %<br>Voltage profile of the out put voltage |   |      |      |      |     |      |      |  |
|---|---|------|------|------|-----|------|------|--|
| Harmonic OrderDC component35791113  |   |      |      |      |     |      |      |  |
| % of fundamental  | 0 | 3.12 | 1.45 | 3.12 | 1.5 | 3.24 | 0.71 |  |

Table 5

| For $f_c = 500$ Hz and MI = 1                    |   |      |      |      |      |      |      |  |  |
|--|---|------|------|------|------|------|------|--|--|
| $V_{OUT} = 188.2 \text{ volts}, (THD)_V = 55 \%$ |   |      |      |      |      |      |      |  |  |
| Voltage profile of the out put voltage           |   |      |      |      |      |      |      |  |  |
| Harmonic OrderDC component35791113               |   |      |      |      |      | 13   |      |  |  |
| % of fundamental                                 | 0 | 1.62 | 0.37 | 1.58 | 0.11 | 0.11 | 0.48 |  |  |

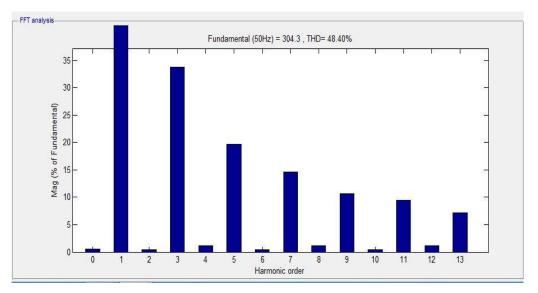


Fig.2: Output voltage Harmonic spectra for  $f_c = 50$  Hz and MI = 1

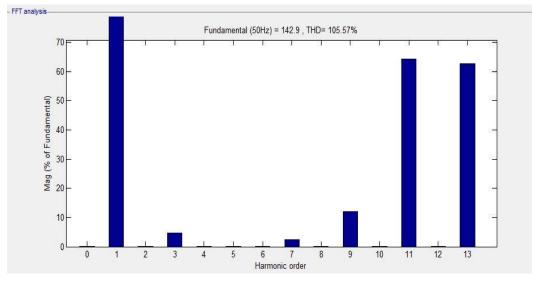


Fig.3: Output voltage Harmonic spectra for  $f_c = 300$  Hz and MI = 0.6

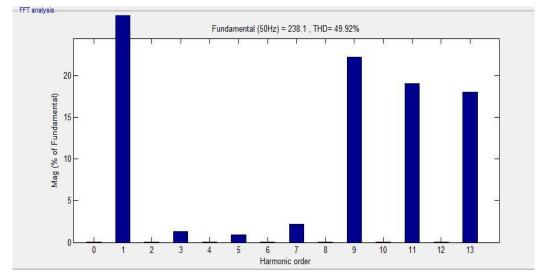


Fig.4: Output voltage Harmonic spectra for  $f_c = 300$  Hz and MI = 1

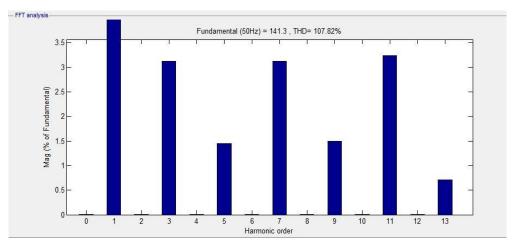


Fig.5: Output voltage Harmonic spectra for  $f_c = 500$  Hz and MI = 0.6

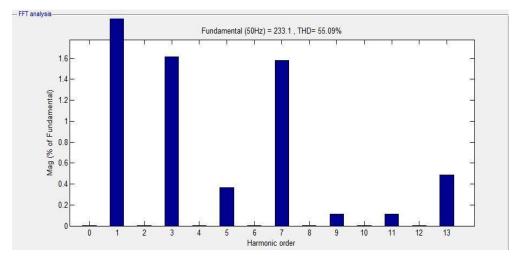


Fig.6: Output voltage Harmonic spectra for  $f_c = 500$  Hz and MI = 1

#### **IV. CONCLUSION**

From the results shown in table 1 to table 5 and harmonic spectra of the output voltage shown in fig.2 to fig.6, following conclusions can be drawn:

1. For a lagging power factor load, the output voltage contains odd harmonics in significant % of the fundamental component. The even harmonics are not in a significant % of fundamental component.

2. To reduce the THD of the output voltage the frequency of carrier signal  $f_c$  and the modulation index MI plays the key role. On changing the (MI) from 0.6 to 1, output voltage THD reduces from 105% to 49% at a carrier frequency 300 Hz. To eliminate any particular order of harmonics carrier frequency  $f_c$  is the key factor. At carrier frequency  $f_c = 300$  Hz, lower order harmonics are reduced as compare to their % for 50 Hz carrier frequency. On changing the modulation index (MI) from 0.6 to 1 on the same carrier frequency, the % of the odd harmonics goes down significantly.

- 3. The same trend of results can also be observed for  $f_c = 500$  Hz and for MI = 0.6 & 1...
- 4. The magnitude of the output voltage varies with change in MI. It increases as MI approaches to the higher value i.e. 1.

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